Homework Solutions 10/3/2007

Problems

39. a.

$$r = r_{earth} + h = 6.38 \cdot 10^{6} m + 2.00 \cdot 10^{5} m = 6.58 \cdot 10^{6} m$$

$$\frac{Gm_{s}m_{R}}{r^{2}} = \frac{m_{s}v^{2}}{r}$$

$$v = \sqrt{\frac{Gm_{E}}{r}} = \sqrt{\frac{\left(6.67 \cdot 10^{-11} \frac{Nm^{2}}{kg^{2}}\right)(5.98 \cdot 10^{24} kg)}{6.58 \cdot 10^{6} m}}$$

$$v = 7.79 \cdot 10^{3} \frac{m}{s}$$

$$v = \frac{d}{t}$$

$$t = \frac{d}{v} = \frac{2\pi r}{v} = \frac{2\pi (6.58 \cdot 10^{6} m)}{7.79 \cdot 10^{3} \frac{m}{s}} = 5.31 \cdot 10^{3} s = 1.48h$$

b.

$$v = 7.79 \bullet 10^3 \, \frac{m}{s}$$

c. If the rocket is launched from the equator, its initial speed is the orbital speed of the earth.

$$v_{i} = \frac{2\pi (6.38 \bullet 10^{6} m)}{86400 s} = 464 \frac{m}{s}$$
$$W = (KE + U_{g})_{f} - (KE + U_{g})_{i}$$

$$U_{s} = mgh$$

$$mg = \frac{Gm_{s}m}{r^{2}}$$

$$U_{s} = \frac{Gm_{s}mh}{r^{2}}$$

$$h = r$$

$$U_{s} = \frac{Gm_{s}m}{r}$$

$$W = \left(\frac{1}{2}mv^{2} + \frac{Gm_{s}m_{s}}{r}\right)_{r} - \left(\frac{1}{2}mv^{2} + \frac{Gm_{s}m_{s}}{r}\right)_{r}$$

$$W = \left(\frac{1}{2}(200kg)\left(7.79 \cdot 10^{3}\frac{m}{s}\right)^{2} + \frac{6.67 \cdot 10^{-11}\frac{Nm^{2}}{kg^{2}}(5.98 \cdot 10^{24}kg)(200kg)}{6.58 \cdot 10^{6}m}\right) - \left(\frac{1}{2}(200kg)\left(464\frac{m}{s}\right)^{2} + \frac{6.67 \cdot 10^{-11}\frac{Nm^{2}}{kg^{2}}(5.98 \cdot 10^{24}kg)(200kg)}{6.38 \cdot 10^{6}m}\right)$$

$$W = 5.67 \cdot 10^{9} J$$
49. a.

$$mg - \eta = \frac{mv^2}{r}$$
$$\eta = mg - \frac{mv^2}{r}$$

$$a_{c} = \frac{v^{2}}{r} = 0.0340 \frac{m}{s^{2}}$$

Since the normal force is the person's perception of her/his weight, that value would be less than their actual weight, mg, by m times 0.0340 m/s/s.

b.

$$\eta = mg - \frac{mv^2}{r}$$

$$\eta = (75.0kg) \left(9.80\frac{m}{s^2}\right) - (75.0kg) \left(0.0340\frac{m}{s^2}\right) = 732N$$

At the Equator a person would feel like s/he weighs 732 N whereas at the poles s/he would feel like s/he weighs 735 N.

c.

$$\eta = mg - \frac{mv^2}{r}$$
$$\eta = (75.0kg) \left(9.80\frac{m}{s^2}\right) = 735N$$

59. a.

$$mgh_{i} + \frac{1}{2}mv_{i}^{2} = mgh_{f} + \frac{1}{2}mv_{f}^{2}$$

$$mgh + \frac{1}{2}mv_{0}^{2} = mg\left(\frac{2}{3}h\right) + \frac{1}{2}mv_{A}^{2}$$

$$v_{A} = \sqrt{2g\left(h - \frac{2}{3}h\right) + (v_{0}^{2})} = \sqrt{2g\left(\frac{h}{3}\right) + (v_{0}^{2})}$$

$$mg = \frac{mv_{A}^{2}}{R}$$

$$v_{A} = \sqrt{gR}$$

$$\sqrt{2g\left(\frac{h}{3}\right) + \left(v_0^2\right)} = \sqrt{gR}$$
$$2g\left(\frac{h}{3}\right) + \left(v_0^2\right) = gR$$
$$v_0^2 = gR - 2g\left(\frac{h}{3}\right)$$
$$v_0 = \sqrt{gR - 2g\left(\frac{h}{3}\right)} = \sqrt{g\left(R - \frac{2h}{3}\right)}$$

b.

$$mgh_{i} + \frac{1}{2}mv_{i}^{2} = mgh_{f} + \frac{1}{2}mv_{f}^{2}$$

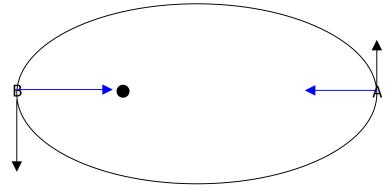
$$mgh + \frac{1}{2}mv_{0}^{2} = mgh'$$

$$h' = \frac{gh + \frac{1}{2}v_{0}^{2}}{g} = \frac{gh + \frac{1}{2}g\left(R - \frac{2h}{3}\right)}{g} = h + \frac{R}{2} - \frac{h}{3}$$

$$h' = \frac{R}{2} + \frac{2h}{3}$$

62. a.

velocity vectors in black, acceleration in blue



b. The velocity vector at B is longer than the velocity vector at A because of conservation of mechanical energy. The potential energy is greater at A so therefore kinetic energy must be greater at B, resulting from a larger velocity as the spacecraft accelerates toward B. The acceleration vector at B is larger than the acceleration vector at B because the net force on the spacecraft is larger at B and from Newton's Second Law we know that net force and acceleration are proportional.